COMPUTER SECURITY

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Cryptography: more advanced topics (cont.)

One-way cryptography

Motivation

● «*Hash functions are everywhere in cryptography — everywhere!*» [1](#page-1-4)

Applications of one-way functions

- data integrity protection
	- \circ *P* public: $F = h(P)$ is characteristic of *P*
- confirmation of knowledge
	- \circ *P* secret: publish $F = h(P)$; later, when *P* is turned public, *F* proves previous knowledge of *P*
- \bullet key derivation
	- known $k1$, $k2 = h(k1)$ is new key that does not compromise $k1$!
- pseudo-random number generation
	- *seed* secret: *h n* (*seed*) is apparently random for any successive *n*
- *...*
- [1](#page-1-3) *Real-World Cryptography*, D. Wong, Manning, 2021

Definitions[1](#page-2-2)

- (minimum) **hash** function H^2 H^2
	- compression: maps input *P* of arbitrary finite bit-length, to output *h* of fixed bit-length
	- ease of computation: for any *P*
- **compression** function^{[3](#page-2-6)}
	- \circ hash function with fixed-size inputs
- **one-way** hash function
	- \circ impractical^{[4](#page-2-8)} to invert function
- **collision-resistant** hash function
	- \circ impractical to find two inputs with same output

- [1](#page-2-1) Somewhat based on *Handbook of Applied Cryptography*, A.J. Menezes et. al., 5th Printing, CRC Press, 2001.
- [2](#page-2-3) can use (secret) keys or not... If unkeyed, are also called MDC (Modification Detection Code) functions.
- [3](#page-2-5) this definition is different from the one commonly adopted - see ahead!
4 impractical = currently computationally infeasible
- $impractical = currently, computationally infeasible$

Simple examples (P = P1 P2 P3... = P1 || P2 || P3...)

• (minimum) **hash** function (*in*, len(*P*); *out*, len(*h*))^{[1](#page-3-1)}

 $h = P_1 \bigoplus P_2 \bigoplus P_3 \bigoplus \ldots$, length (P_i) = length (h)

- **compression** function (*in*: *m* bits ; *out*: *n* bits)
	- \circ *out* = (*in*'s first *n* bits) \oplus (*in*'s last (*m*-*n*) bits || (2*n*-*m*) 0 bits)
- **one-way** hash function (*in*: *m* bits ; *out*: *n* bits)

 $h = P \mod \text{len}(h)$

collision-resistant hash function

 \circ ?...

[1](#page-3-0) len --> length

Note on compression function's definition:

- here adopted definition:
	- Compression function (*in*: *m* bits ; *out*: *n* bits)
- common used definition:
	- Common "Compression" function (*in*: *b* bits, *n* bits ; *out*: *n* bits)

Fig. a) Adopted definition of Compression function; b) Commonly defined "Compression" function.

Construction of hash functions

- • iterated hash functions (e.g. Merkle–Damgård construction) [FIG]
	- block cipher based hash functions (e.g. Davies-Meyer construction) [FIG]
		- using existing secure cipher functions
	- customized (e.g. SHA-1)
		- specifically designed "from scratch" for optimized performance
	- \circ modular arithmetic based^{[1](#page-5-2)} (e.g. MASH-1)
		- quite few implementations as research interest is low:
			- sluggish relative to customized hash functions
			- «*embarrassing history of insecure proposals*» (Menezes et al.)
	- sponge constructions (e.g. SHA-3) [FIG]
		- new paradigm, allowing easy adjustment of output length

[1](#page-5-1) ISO/IEC 10118-4:1998, Hash-functions using modular arithmetic

Fig. Two views of the Merkle–Damgård construction: a) software-view ; b) time-view.

...One-way cryptography (cont.): Block cipher based - Davies-Meyer construction

Fig. Structure of Davies-Meyer construction (block-cipher based): a) enciphering snippet with general idea: if *in* is fixed, *Ekey* is one-way for mapping *key --> out* ! b) Davies-Meyer construction: final hashing result is iteration for all *Pi* blocks .

...One-way cryptography (cont.)

Case study (simplified): SHA-3 (sponge construction)

sponge

Fig. Sponge construct (time-view): *M* is input that, after padding, is divided in blocks of *r* (rate) bits; *Z* is output of *l* bits of length (specified by input parameter), concatenation of *r* bits' blocks; *c* is capacity, inner, never output, state bits. (*in* keccak.team/sponge_duplex.html)

...One-way cryptography (cont.): SHA-3 (sponge construction)

Sponge construction (cont.)

- function Keccak- $f[1600]$ $f[1600]$ $f[1600]$ ¹:
	- group of permutations on
	- \circ internal state: *b* bits (5 \times 5 \times 2⁶ bits = 1600)
	- $b = r + c$ bits
		- *r*: bits affected by input
		- *c*: always internal bits
	- group permutation:
		- \blacksquare 12 + 2×6 rounds of five steps:
			- θ ρ π χ ι
- specific padding rules
- Fig. Inner aspects of sponge structure: a) bits of state; b) sponge function operations.
- Keccak is pronounced as "ketchak" ([keccak.team/keccak_specs_summary.html\)](https://keccak.team/keccak_specs_summary.html).

...One-way cryptography (cont.)

Overall weaknesses of irreversible systems

Problem:

- The number produced by the hashing operation is usually fixed (finite)
	- So, there **have to be** collisions, in an infinite universe of inputs!
	- Will they be likely or easy to cause?

Answer:

- that depends
	- on the randomness of the values resulting from the operation
	- \circ on the size of those values (number of bits)
	- \circ on the intended application

...One-way cryptography: *Irreversible (cont.)*

Attacks

- certain: only brute force! (if one can live for enough time...)
	- \circ the intention is to find an entry with a specific result?
		- try 2*ⁿ* inputs (*n*, number of bits of *hash*)
- likely: perhaps by using certain curious techniques...
	- \circ the intention is to find two entries with the same result?
		- **birthday attack:** try $\sqrt{2^n} = 2^{n/2}$ inputs for 50% chance of success
		- 2 sets of documents with the same *hash*: one "good" set, one "evil"!^{[1](#page-11-1)}
- possible: scientifically search for construction weaknesses
	- research, research, research
		- MD5: [MD5 considered harmful today](https://www.win.tue.nl/hashclash/rogue-ca/)
		- SHA-1: [We have broken SHA-1 in practice](https://shattered.io/)
		- **...**

Diversity of possibilities for trying different documents are as simple as varying the number of spaces between words...

...One-way cryptography: *Irreversible (cont.)*

Ideal strength of hash function of n-bit output:

- security is as good as a random oracle with output truncated to *n* bits
- implies resistance of size:
	- \circ $2^{n/2}$ for strong collision attacks
	- 2^{*n*} for weak collision attacks

Example: sponge construction (SHA-3) strength

- with random permutation: as strong as a random oracle
- capacity *c* determines resistance size:
	- 2^{*c*} for both strong and weak collision attacks
		- **■** unfortunately, security is traded for speed, for constant $b (= r+c)$ size
			- higher security (*c*), lower speed (more *r*-bit input blocks to process)

Integrity & Confidentiality protection

- fact: (*confidentiality*) operation modes do not guarantee *integrity* protection^{[1](#page-13-2)}
- so, some type of integrity protection must be added
	- basic example: combine secrecy with digital signatures [FIG]
	- in general: use *authenticated encipherment* protocols

Fig. Confidentiality with integrity protection.

[1](#page-13-1) E.g. for CBC operation mode, see Kaufman et. al, Network Security, pp. 98-101. Exercise: show the vulnerability with *One time pad*!

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(\underline{ToC}) 14-27
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...Integrity Protection (cont.)...

Authenticated ciphering protocols (modes)[1](#page-14-2)

- • special protocols developed to aggregate both protections
	- \circ in general, integrity protection is provided by Message Integrity^{[2](#page-14-4)} Codes
	- but digital signing can also be used (of course) [previous FIG]
- the main approaches are:
	- \circ (external) combination of protective techniques^{[3](#page-14-6)}
		- prone to vulnerabilities due to incorrect implementation
	- \circ "intrinsic" combination
		- several standardized schemes
		- sponge functions can be used in *duplex mode!*
		- *signcryption*: "low-cost" combination of digital signing and ciphering^{[4](#page-14-8)}
- [1](#page-14-1) *Authenticated Encryption with Associated Data* (AEAD) applies when it is explicitly necessary to assure integrity protection of plaintext data that is to accompany ciphertext (e.g. network packets might need a visible header that should be integrity protected as well as the secret payload).
- [2](#page-14-3) or Authentication ;-)
- [3](#page-14-5) also called "generic composition" of schemes used separately for achieving confidentiality and integrity protection
- [4](#page-14-7) Digital Signcryption or How to Achieve Cost(Signature & Encryption)..., Y. Zheng, CRYPTO '97

...Integrity Protection with Authenticated Modes...

Authenticated Modes - "generic composition"

Encrypt-then-MAC, EtM

- ISO/IEC 19772:2009
- process: [FIG *in* Wikipedia]
	- 1st, encipher; 2nd, calculate MIC
	- non-parallelizable
- different keys K_E , K_{MAC} !
- "normal" padding
- reverse process:
	- verify integrity of ciphertext; decipher to get plaintext
	- parallelizable
- considered the more secure method (compared with the following)^{[1](#page-15-1)}

...Integrity Protection with Authenticated Modes - "generic composition" (cont.)

Encrypt-and-MAC (E&M)

- process: [FIG *in* Wikipedia]
	- encipher; calculate MIC
	- parallelizable
- apparently, a single key is enough!
- "normal" padding
- reverse process:
	- 1st, decipher to get plaintext; 2nd, verify integrity of plaintext
	- non-parallelizable

...Integrity Protection with Authenticated Modes - "generic composition" (cont.)

MAC-then-Encrypt (MtE)

- process: [FIG *in* Wikipedia]
	- 1st, calculate MIC; 2nd, encipher
	- non-parallelizable
- apparently, a single key is enough!
- padding after hashing
- reverse process:
	- 1st, decipher to get plaintext and MAC; 2nd, verify integrity of plaintext
	- non-parallelizable

...Integrity Protection with Authenticated Modes (cont.)

Authenticated Modes - "intrinsic"

- here, there is an integration of the 2 protections
	- the schemes are built with provision to provide both
- the usual procedure is
	- use a primary key (*seed*) to feed an extended key-generation function
	- use the generated long key, to encipher *P* in *stream* mode
		- typically, a variant of Counter Mode is used [FIG]
	- \circ use part of the generated key to produce a MIC of the ciphered (or plain) text

...Integrity Protection with Authenticated Modes - "intrinsic" (cont.)

Some "famous" examples

Galois/Counter Mode (GCM)

- NIST 800-38D
- process: [FIG]
- confidentiality:
	- AES-128b is typical
- integrity protection: GMAC [FIG next page]
	- \circ ciphertext + Associated Data
- apparently, highly performative (parallelization by inter-leaving & pipelining?)
- some obs:
	- *AD* and *C* are padded separately before being concatenated; *IV* is used sequentially in GMAC first and then in CTR; internal intermediate states are to be kept private

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...Integrity Protection with Authenticated Modes - "intrinsic"

ChaCha20-Poly1305

- **RFC 8439**
- designed by D. J. Bernstein
	- \circ ChaCha20^{[1](#page-21-1)} stream cipher
	- Poly1305 *authenticator*
- process: [FIG]
	- key stream feeds message integrity code function first (counter=0) and then XOR cipher (counter>0)
	- *AD* and *C* are padded separately before being concatenated

20-round version of ChaCha

...Integrity Protection with Authenticated Modes - "intrinsic": ChaCha20-Poly1305

ChaCha20-Poly1305 (cont.): Chacha20

- input: 32B (256b) key, 12B (96b) IV (*nonce*), 4B (32b) counter [FIG]
- output: stream key in 64B (512b) blocks
- internal state: $4 \times 4 \times 4B$ (16 32b-integers) = 64 B (512b)
- block function: [FIG]
	- sequence of 10 double "quarter"-rounds
	- quarter-round: set of operations on 4 numbers (addition modulo 2³² , XOR, left-shift of *n* bits)
	- \circ final sum with input
- encipher algorithm:
	- for each iteration (increasing counter), use key stream to cipher 64B block of Plaintext
- deciphering is obvious

state (4x4 32b ints) in:

Cnst Cnst Cnst Cnst Key Key Key Key Key Key Key Key Ctr IV IV IV

Cnst Cnst Cnst Cnst: "expa" "nd 3" "2-by" "te k"

...Integrity Protection with Authenticated Modes - "intrinsic": ChaCha20-Poly1305

ChaCha20-Poly1305 (cont.): Poly1305

- input:
	- 32B (256b) **one-time**, two-part key: *r* (16B) || *s* (16B)
	- arbitrary-length message
- output: 16B (128b) MAC
- arithmetic operations with 16B groups used as numbers

Fig. D. J. Bernstein's Poly1305 *authenticator*: 128b MAC.

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...Integrity Protection with Authenticated Modes – "intrinsic"

SpongeWrap

sponge construct in duplex mode

Fig. Sponge construct in duplex-mode for authenticated enciphering (AEAD): notice that plaintext *P* is XORed, block by block, with ƒ's outputs - the *keystream, ki !* The function *pad* is used for padding blocks.

Exercise: adapt the picture to a stream cipher in which the "sponge" generates the key(s).

(to be continued...)

Pointers...

- "**Block cipher mode of operation**", -2024 Wikipedia o en.wikipedia.org/wiki/Block cipher_mode_of_operation
- "**Recommendation for Block Cipher Modes of Operation: Galois/Counter Mode (GCM) and GMAC**", 2007 – M. Dworkin, NIST
	- ○ nvlpubs.nist.gov/nistpubs/Legacy/SP/nistspecialpublication800-38d.pdf
- "**The Poly1305-AES Message-Authentication Code**", 2005 D. Bernstein
	- \circ link.springer.com/content/pdf/10.1007/11502760 3.pdf
- "**ChaCha, a variant of Salsa20**", 2008 D. Bernstein
	- ○ cr.yp.to/chacha/chacha-20080120.pdf
- "**Duplexing the sponge: single-pass authenticated encryption...**", 2011 G. Bertoni, J. Daemen, M. Peeters, G.Van Assche
	- ○ eprint.iacr.org/2011/499.pdf
- "**The sponge and duplex constructions**", -2023, G. Bertoni, J. Daemen, S. Hoffert, M. Peeters, G. Van Assche, R. Van Keer
	- ○ keccak.team/sponge_duplex.html

