# COMPUTER SECURITY

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# Cryptography: more advanced topics (cont.)

# One-way cryptography

Motivation

• «Hash functions are everywhere in cryptography — everywhere!»<sup>1</sup>

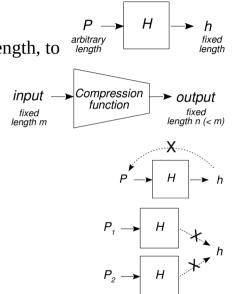
# **Applications of one-way functions**

- data integrity protection
  - *P* public:  $\vec{F} = h(P)$  is characteristic of *P*
- confirmation of knowledge
  - *P* secret: publish F = h(P); later, when *P* is turned public, *F* proves previous knowledge of *P*
- key derivation
  - known k1, k2 = h(k1) is new key that does not compromise k1!
- pseudo-random number generation
  - *seed* secret: *h*<sup>*n*</sup>(*seed*) is apparently random for any successive *n*
- ...
- Real-World Cryptography, D. Wong, Manning, 2021



## **Definitions**<sup>1</sup>

- (minimum) hash function  $H^2$ 
  - compression: maps input *P* of arbitrary finite bit-length, to output *h* of fixed bit-length
  - $\circ$  ease of computation: for any *P*
- **compression** function<sup>3</sup>
  - hash function with fixed-size inputs
- **one-way** hash function
  - impractical<sup>4</sup> to invert function
- collision-resistant hash function
  - $\circ$  impractical to find two inputs with same output



- 1 Somewhat based on Handbook of Applied Cryptography, A.J. Menezes et. al., 5th Printing, CRC Press, 2001.
- 2 can use (secret) keys or not... If unkeyed, are also called MDC (Modification Detection Code) functions.
- 3 this definition is different from the one commonly adopted see ahead!
- 4 impractical = currently, computationally infeasible

Simple examples ( $P = P_1 P_2 P_3... = P_1 || P_2 || P_3...$ )

• (minimum) **hash** function (*in*, len(*P*); *out*, len(*h*))<sup>1</sup>

•  $h = P_1 \bigoplus P_2 \bigoplus P_3 \bigoplus \dots$ , length  $(P_i) = \text{length}(h)$ 

- **compression** function (*in*: *m* bits ; *out*: *n* bits)
  - out = (in's first *n* bits)  $\oplus$  (in's last (*m*-*n*) bits || (2*n*-*m*) 0 bits)
- **one-way** hash function (*in*: *m* bits ; *out*: *n* bits)

•  $h = P \mod \operatorname{len}(h)$ 

• **collision-resistant** hash function

o **?...** 

1 len --> length



### Note on compression function's definition:

- here adopted definition:
  - Compression function (*in*: *m* bits ; *out*: *n* bits)
- common used definition:
  - Common "Compression" function (*in*: *b* bits, *n* bits ; *out*: *n* bits)

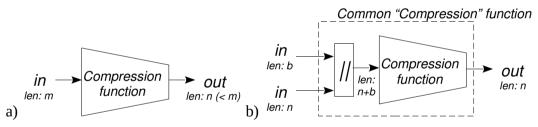


Fig. a) Adopted definition of Compression function; b) Commonly defined "Compression" function.



### **Construction of hash functions**

- iterated hash functions (e.g. Merkle–Damgård construction) [FIG]
  - block cipher based hash functions (e.g. Davies-Meyer construction) [FIG]
    - using existing secure cipher functions
  - customized (e.g. SHA-1)
    - specifically designed "from scratch" for optimized performance
  - modular arithmetic based<sup>1</sup> (e.g. MASH-1)
    - quite few implementations as research interest is low:
      - sluggish relative to customized hash functions
      - *«embarrassing history of insecure proposals»* (Menezes et al.)
  - $\circ$  sponge constructions (e.g. SHA-3) [FIG]
    - new paradigm, allowing easy adjustment of output length

1 ISO/IEC 10118-4:1998, Hash-functions using modular arithmetic





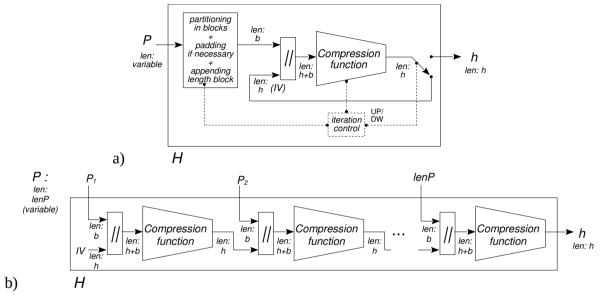


Fig. Two views of the Merkle–Damgård construction: a) software-view ; b) time-view.



...One-way cryptography (cont.): Block cipher based - Davies-Meyer construction

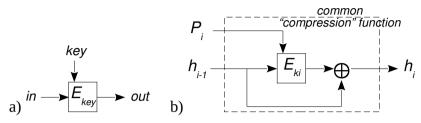
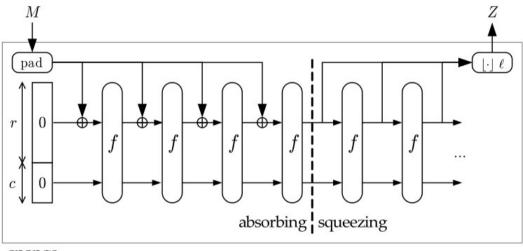


Fig. Structure of Davies-Meyer construction (block-cipher based):
a) enciphering snippet with general idea: if *in* is fixed, *E*<sub>key</sub> is one-way for mapping *key* --> *out* !
b) Davies-Meyer construction: final hashing result is iteration for all *P*<sub>i</sub> blocks .



...One-way cryptography (cont.)

**Case study (simplified): SHA-3 (sponge construction)** 



sponge

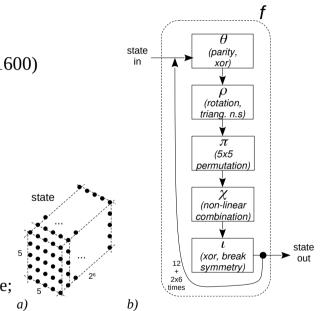
Fig. Sponge construct (time-view): *M* is input that, after padding, is divided in blocks of *r* (rate) bits; *Z* is output of *l* bits of length (specified by input parameter), concatenation of *r* bits' blocks; *c* is capacity, inner, never output, state bits. (*in* <u>keccak.team/sponge\_duplex.html</u>)

...One-way cryptography (cont.): SHA-3 (sponge construction)

### Sponge construction (cont.)

- function Keccak-*f*[1600]<sup>1</sup>:
  - $\circ$  group of permutations on
  - internal state: *b* bits ( $5 \times 5 \times 2^6$  bits = 1600)
  - b = r + c bits
    - *r*: bits affected by input
    - *c*: always internal bits
  - group permutation:
    - $12 + 2 \times 6$  rounds of five steps:  $\theta \rho \pi \chi \iota$
- specific padding rules
- Fig. Inner aspects of sponge structure: a) bits of state; b) sponge function operations.
- 1 Keccak is pronounced as "ketchak" (<u>keccak.team/keccak\_specs\_summary.html</u>).

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...One-way cryptography (cont.)

# **Overall weaknesses of irreversible systems**

### Problem:

- The number produced by the hashing operation is usually fixed (finite)
  - So, there **have to be** collisions, in an infinite universe of inputs!
  - Will they be likely or easy to cause?

### Answer:

- that depends
  - $\circ ~~$  on the randomness of the values resulting from the operation
  - $\circ~$  on the size of those values (number of bits)
  - $\circ$  on the intended application



...One-way cryptography: Irreversible (cont.)

### Attacks

- certain: only brute force! (if one can live for enough time...)
  - the intention is to find an entry with a specific result?
    - try 2<sup>n</sup> inputs (n, number of bits of hash)
- likely: perhaps by using certain curious techniques...
  - $\circ$  the intention is to find two entries with the same result?
    - **birthday attack**: try  $\sqrt{2^n} = 2^{n/2}$  inputs for 50% chance of success
    - 2 sets of documents with the same *hash*: one "good" set, one "evil"!<sup>1</sup>
- possible: scientifically search for construction weaknesses
  - research, research, research
    - MD5: <u>MD5 considered harmful today</u>
    - SHA-1: <u>We have broken SHA-1 in practice</u>
    - **...**

1 Diversity of possibilities for trying different documents are as simple as varying the number of spaces between words...



### ...One-way cryptography: Irreversible (cont.)

### Ideal strength of hash function of n-bit output:

- security is as good as a random oracle with output truncated to *n* bits
- implies resistance of size:
  - $2^{n/2}$  for strong collision attacks
  - 2<sup>*n*</sup> for weak collision attacks

### Example: sponge construction (SHA-3) strength

- with random permutation: as strong as a random oracle
- capacity *c* determines resistance size:
  - $\circ$  2<sup>*c*</sup> for both strong and weak collision attacks
    - unfortunately, security is traded for speed, for constant b (= r+c) size
      - higher security (*c*), lower speed (more *r*-bit input blocks to process)



# Integrity & Confidentiality protection

- fact: (*confidentiality*) operation modes do not guarantee *integrity* protection<sup>1</sup>
- so, some type of integrity protection must be added
  - basic example: combine secrecy with digital signatures [FIG]
  - in general: use *authenticated encipherment* protocols

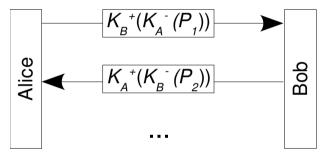


Fig. Confidentiality with integrity protection.

1 E.g. for CBC operation mode, see Kaufman et. al, Network Security, pp. 98-101. Exercise: show the vulnerability with One time pad!

...Integrity Protection (cont.)...

# Authenticated ciphering protocols (modes)<sup>1</sup>

- special protocols developed to aggregate both protections
  - in general, integrity protection is provided by Message Integrity<sup>2</sup> Codes
  - but digital signing can also be used (of course) [previous FIG]
- the main approaches are:
  - (external) combination of protective techniques<sup>3</sup>
    - prone to vulnerabilities due to incorrect implementation
  - "intrinsic" combination
    - several standardized schemes
    - sponge functions can be used in *duplex mode*!
    - signcryption: "low-cost" combination of digital signing and ciphering<sup>4</sup>
- 1 *Authenticated Encryption with Associated Data* (AEAD) applies when it is explicitly necessary to assure integrity protection of plaintext data that is to accompany ciphertext (e.g. network packets might need a visible header that should be integrity protected as well as the secret payload).
- 2 or Authentication ;-)
- 3 also called "generic composition" of schemes used separately for achieving confidentiality and integrity protection
- 4 Digital Signcryption or How to Achieve Cost(Signature & Encryption)..., Y. Zheng, CRYPTO '97

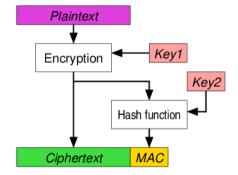


...Integrity Protection with Authenticated Modes...

### Authenticated Modes - "generic composition"

### Encrypt-then-MAC, EtM

- ISO/IEC 19772:2009
- process: [FIG *in* Wikipedia]
  - $\circ$   $\,$  1st, encipher; 2nd, calculate MIC  $\,$
  - non-parallelizable
- different keys  $K_E$ ,  $K_{MAC}$  !
- "normal" padding
- reverse process:
  - verify integrity of ciphertext; decipher to get plaintext
  - parallelizable
- considered the more secure method (compared with the following)<sup>1</sup>
- 1 see, for instance, Bellare & Namprempre "Authenticated Encryption: Relations among Notions and Analysis of the Generic Composition Paradigm" (2008)

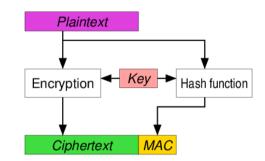


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...Integrity Protection with Authenticated Modes - "generic composition" (cont.)

### Encrypt-and-MAC (E&M)

- process: [FIG *in* Wikipedia]
  - $\circ$  encipher; calculate MIC
  - parallelizable
- apparently, a single key is enough!
- "normal" padding
- reverse process:
  - 1st, decipher to get plaintext;
     2nd, verify integrity of plaintext
  - non-parallelizable

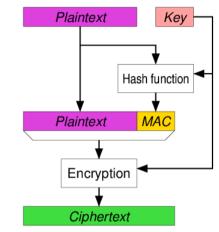




...Integrity Protection with Authenticated Modes - "generic composition" (cont.)

### MAC-then-Encrypt (MtE)

- process: [FIG *in* Wikipedia]
  - $\circ$  1st, calculate MIC; 2nd, encipher
  - o **non-parallelizable**
- apparently, a single key is enough!
- padding after hashing
- reverse process:
  - 1st, decipher to get plaintext and MAC; 2nd, verify integrity of plaintext
  - non-parallelizable

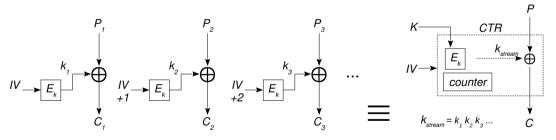




...Integrity Protection with Authenticated Modes (cont.)

### Authenticated Modes - "intrinsic"

- here, there is an integration of the 2 protections
  - $\circ$  the schemes are built with provision to provide both
- the usual procedure is
  - use a primary key (*seed*) to feed an extended key-generation function
  - $\circ$  use the generated long key, to encipher *P* in *stream* mode
    - typically, a variant of Counter Mode is used [FIG]
  - $\circ~$  use part of the generated key to produce a MIC of the ciphered (or plain) text



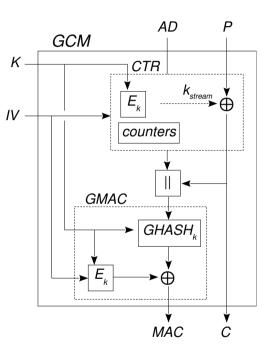
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...Integrity Protection with Authenticated Modes - "intrinsic" (cont.)

### Some "famous" examples

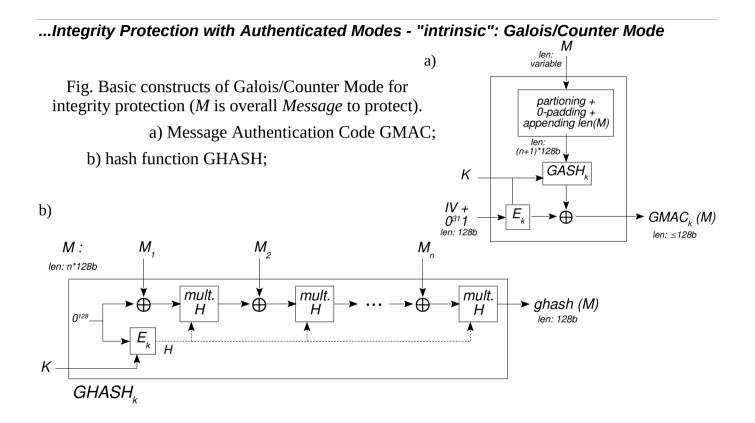
### Galois/Counter Mode (GCM)

- NIST 800-38D
- process: [FIG]
- confidentiality:
  - AES-128b is typical
- integrity protection: GMAC [FIG next page]
  - ciphertext + Associated Data
- apparently, highly performative (parallelization by inter-leaving & pipelining?)
- some obs:
  - *AD* and *C* are padded separately before being concatenated; *IV* is used sequentially in GMAC first and then in CTR; internal intermediate states are to be kept private



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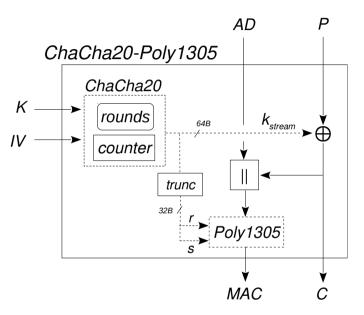


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...Integrity Protection with Authenticated Modes - "intrinsic"

### ChaCha20-Poly1305

- RFC 8439
- designed by D. J. Bernstein
  - $\circ$  ChaCha20<sup>1</sup> stream cipher
  - Poly1305 authenticator
- process: [FIG]
  - key stream feeds message integrity code function first (counter=0) and then XOR cipher (counter>0)
  - *AD* and *C* are padded separately before being concatenated



1 20-round version of ChaCha

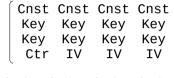


...Integrity Protection with Authenticated Modes - "intrinsic": ChaCha20-Poly1305

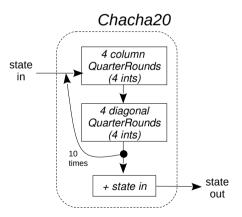
### ChaCha20-Poly1305 (cont.): Chacha20

- input: 32B (256b) key, 12B (96b) IV (*nonce*), 4B (32b) counter [FIG]
- output: stream key in 64B (512b) blocks
- internal state: 4 x 4 x 4B (16 32b-integers) = 64 B (512b)
- block function: [FIG]
  - $\circ$  sequence of 10 double "quarter"-rounds
  - quarter-round: set of operations on 4 numbers (addition modulo  $2^{32}$ , XOR, left-shift of *n* bits)
  - $\circ$  final sum with input
- encipher algorithm:
  - for each iteration (increasing counter), use key stream to cipher 64B block of Plaintext
- deciphering is obvious

state (4x4 32b ints) in:



Cnst Cnst Cnst Cnst: "expa" "nd 3" "2-by" "te k"

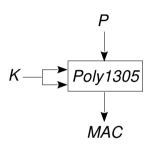




...Integrity Protection with Authenticated Modes - "intrinsic": ChaCha20-Poly1305

#### ChaCha20-Poly1305 (cont.): Poly1305

- input:
  - 32B (256b) **one-time**, two-part key: *r* (16B) || *s* (16B)
  - arbitrary-length message
- output: 16B (128b) MAC
- arithmetic operations with 16B groups used as numbers



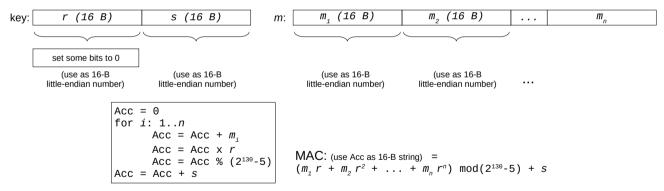


Fig. D. J. Bernstein's Poly1305 authenticator: 128b MAC.

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...Integrity Protection with Authenticated Modes - "intrinsic"

#### SpongeWrap

• sponge construct in duplex mode

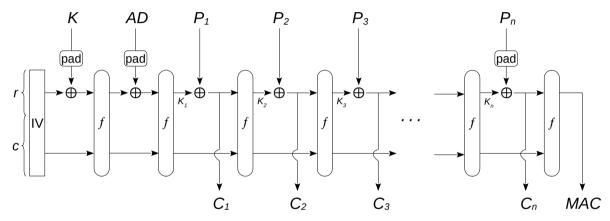


Fig. Sponge construct in duplex-mode for authenticated enciphering (AEAD): notice that plaintext P is XORed, block by block, with f's outputs - the *keystream*,  $k_i$ ! The function *pad* is used for padding blocks.

Exercise: adapt the picture to a stream cipher in which the "sponge" generates the key(s).

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( to be continued...)



# Pointers...

- **"Block cipher mode of operation"**, -2024 Wikipedia
  - en.wikipedia.org/wiki/Block cipher mode of operation
- "Recommendation for Block Cipher Modes of Operation: Galois/Counter Mode (GCM) and GMAC", 2007 M. Dworkin, NIST
  - <u>nvlpubs.nist.gov/nistpubs/Legacy/SP/nistspecialpublication800-38d.pdf</u>
- "The Poly1305-AES Message-Authentication Code", 2005 D. Bernstein
  - <u>link.springer.com/content/pdf/10.1007/11502760\_3.pdf</u>
- "ChaCha, a variant of Salsa20", 2008 D. Bernstein
   cr.yp.to/chacha/chacha-20080120.pdf
- **"Duplexing the sponge: single-pass authenticated encryption...**", 2011 G. Bertoni, J. Daemen, M. Peeters, G.Van Assche
  - eprint.iacr.org/2011/499.pdf
- **"The sponge and duplex constructions**", -2023, G. Bertoni, J. Daemen, S. Hoffert, M. Peeters, G. Van Assche, R. Van Keer
  - <u>keccak.team/sponge\_duplex.html</u>

